| 11 | 2b | The function $f(x)=\cos 2 x-x$ has a zero near $x=\frac{1}{2}$. Use one Newton's method to obtain another approximation to this zero correct to two decimal places. | 3 |
| :---: | :---: | :---: | :---: |
|  |  | Let $f(x)=\cos 2 x-x$ $f^{\prime}(x)=-2 \sin 2 x-1$ $\begin{aligned} \therefore f\left(\frac{1}{2}\right) & =\cos 2\left(\frac{1}{2}\right)-\left(\frac{1}{2}\right) \\ & =0.0403 \ldots \\ \therefore f^{\prime}\left(\frac{1}{2}\right) & =-2 \sin 2\left(\frac{1}{2}\right)-1 \\ & =-2.6829 \ldots \end{aligned}$ $\text { Newton's Method: } \quad \begin{aligned} x_{1} & =x_{0}-\frac{f\left(x_{0}\right)}{f^{\prime}\left(x_{0}\right)} \\ & =\frac{1}{2}-\frac{0.0403}{-2.6829} \\ & =0.515 \ldots \\ & =0.52(2 \mathrm{dec} \mathrm{pl}) \end{aligned}$ | State Mean $2.11 / 3$ |

* These solutions have been provided by projectmaths and are not supplied or endorsed by the Board of Studies


## Board of Studies: Notes from the Marking Centre

This proved to be the most challenging part in Question 2. In many responses, candidates did not apply the Table of Standard Integrals to differentiate correctly, nor quote the correct formula for Newton's Method, nor substitute into the formula and evaluate correctly nor remember to use radian mode.
Source: http://www.boardofstudies.nsw.edu.au/hsc exams/

