TG 8 It is given that $40 \%$ of voters support the Stats Party. One hundred and fifty voters are selected at random. Use a suitable approximation to find the probability that more than 55 of the 150 voters support the Stats Party. Projectmaths has provided this probability table extract:

| z | .00 | .01 | .02 | .03 | .04 | .05 | .06 | .07 | .08 | .09 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.5 | .6915 | .6950 | .6985 | .7019 | .7054 | .7088 | .7123 | .7157 | .7190 | .7224 |
| 0.6 | .7257 | .7291 | .7324 | .7357 | .7389 | .7422 | .7454 | .7486 | .7517 | .7549 |
| 0.7 | .7580 | .7611 | .7642 | .7673 | .7704 | .7734 | .7764 | .7794 | .7823 | .7852 |
| 0.8 | .7881 | .7910 | .7939 | .7967 | .7995 | .8023 | .8051 | .8078 | .8106 | .8133 |
| 0.9 | .8159 | .8186 | .8212 | .8238 | .8264 | .8289 | .8315 | .8340 | .8365 | .8389 |

$$
\begin{aligned}
& n=150 \\
& P(\text { support })=p=0.4 \\
& n p=150(0.4)=60
\end{aligned}
$$

As $n p \geq 10$, then use normal distribution:

$$
\begin{aligned}
\mu_{\hat{p}} & =p=0.4 \\
\sigma_{\hat{p}} & =\sqrt{\frac{p(1-p)}{n}} \\
& =\sqrt{\frac{0.4(1-0.4)}{150}} \\
& =0.04
\end{aligned}
$$

Now, 55 out of 150 is 0.3667 . ( 4 dec pl )

$$
\begin{aligned}
z & =\frac{x-\mu}{\sigma} \\
& =\frac{0.3667-0.4}{0.04} \\
& =-0.83(2 \text { dec } \mathrm{pl})
\end{aligned}
$$

For $z=0.83$, the table provides 0.7967 .
Hence, for $z=-0.83$, the table would show 0.2033 .
As $1-0.2033$ is 0.7967 , the probability is 0.7967 .

* These solutions have been provided by projectmaths and are not supplied or endorsed by NESA.

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